

# Sample Size Calculation in Animal Studies Using Resource Equation Approach

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## Abstract

**Animal research plays an important role in the pre-clinical phase of clinical trials. In animal studies, the power analysis approach to sample size calculation is recommended. Whenever it is not possible to assume the standard deviation and the effect size, an alternative to the power analysis approach is the ‘resource equation’ approach, which sets the acceptable range of the error degrees of freedom (DF) in an analysis of variance (ANOVA). The aim of this article is to guide researchers in calculating the minimum and maximum numbers of animals required in animal research by reformulating the error DF formulas.**

**Keywords:** animal research, research design, sample size

## Introduction

Prior to embarking on clinical drug trials on humans, researchers need to conduct extensive pre-clinical studies in vitro (test tube or cell cultures) and in vivo (animal experiments) to examine preliminary efficacy, toxicity, and pharmacokinetics (1). Pre-clinical animal studies should closely follow the established practices in human clinical trials (2). While sample size determination has been adequately highlighted in human clinical studies, it has not adequately been described in animal studies in the published literature (3).

Animal study researchers may face problems in determining how many animals they should use, where a too small sample size can miss the real effect in an experiment, while a sample size that is larger than necessary will lead to wasting resources and ethical issues on the sacrificed animals. Similar to human studies, the power analysis approach

to sample size determination is often the most scientifically favored method. The emphasis on this approach can be clearly seen in a number of papers on methods in animal research (4, 5, 6) and recommendations by animal research committees (7, 8). However, a researcher must have prior knowledge and information about two major concepts in the power analysis approach: 1). effect size (the minimum difference between two groups that can be considered clinically significant) and 2). standard deviation (the measure of variability within a sample for a quantitative variable). The information may not be readily available in the literature or difficult to estimate, especially for studies that are exploratory in nature.

An alternative to the power analysis approach for determining the sample size in animal study is the ‘resource equation’ approach (4, 6, 9, 10). Based on this approach, the acceptable range of degrees of freedom (DF) for the error term in an analysis of variance

(ANOVA) is between 10 to 20 (4, 9, 10). The resource equation approach is suitable for exploratory studies whenever it is not possible to assume the standard deviation and the effect size (4). This is applicable whenever the outcome is a quantitative variable and suitable for analysis by ANOVA.

The aim of this article is to guide researchers on sample size calculation in exploratory animal research. The sample size calculation will be based on the resource equation. This article takes a different approach than the ones presented in other papers (4, 6) in calculating the appropriate number of animals in a study. Using simple algebra, the DF formulas are presented in forms of minimum and maximum numbers of animals required in a study using three common ANOVA designs.

### Minimum and Maximum Sample Sizes for Three ANOVA Designs

#### Design 1: Group comparison—one-way ANOVA

For one-way ANOVA, the between-subject error DF (that is, the within-subject DF) is calculated as:

$$DF = N - k = kn - k = k(n - 1),$$

where  $N$  = total number of subjects,  $k$  = number of groups, and  $n$  = number of subjects per group.

By rearranging the formula,  $n$  is given as:

$$n = DF/k + 1$$

Based on the acceptable range of the DF, the DF in the formulas are replaced with the minimum (10) and maximum (20) DFs to obtain the minimum and maximum numbers of animals per group:

$$\text{Minimum } n = 10/k + 1$$

$$\text{Maximum } n = 20/k + 1$$

In total, the minimum and maximum numbers of animals required are:

$$\text{Minimum } N = \text{Minimum } n \times k$$

$$\text{Maximum } N = \text{Maximum } n \times k$$

For example, in a study to compare the tumor sizes (in cm, change = post-treatment size – pre-treatment size) between three treatment groups (honey, honey with chemical, and control), the sample sizes per group are

Minimum  $n = 10/3 + 1 = 4.3 =$  rounded up to 5 animals/group

Maximum  $n = 20/3 + 1 = 7.7 =$  rounded down to 7 animals/group.

Please note that the minimum and maximum numbers of animals per group are rounded up and down, respectively, to keep the DF for each sample size/group within the limit (e.g., DF = 12 for  $n = 5$ , and DF = 18 for  $n = 7$ ).

The total sample sizes are:

Minimum  $N = \text{Minimum } n \times 3 = 5 \times 3 =$  15 animals

Maximum  $N = \text{Maximum } n \times 3 = 7 \times 3 =$  21 animals

In conclusion, for the proposed study, between 5 and 7 animals per group are required. In other words, a total of 15 to 21 animals are required to keep the DF within the range of 10 to 20.

Although the formula is given for one-way ANOVA, it is also applicable for an independent  $t$ -test (involving two groups). In this case,  $k$  is set equal to 2. The formula is applicable because the error DF of one-way ANOVA and the DF for an independent  $t$ -test is equal for a two-group comparison. Performing one-way ANOVA and an independent  $t$ -test (assuming equal variance) will also result in the same  $P$ -value.

#### Design 2: Same subjects, repeated measures— one within factor, repeated-measures ANOVA

For this repeated-measures ANOVA design, only one group of subjects is involved. That is why it is concerned only with the within-subject factor. The within-subject error DF is calculated as:

$$DF = (N - 1)(r - 1),$$

where  $N$  = total number of subjects and  $r$  = number of repeated measurements. Because there is no grouping factor, the calculation of  $n$  is not applicable here.

$N$  is obtained as:

$$N = DF/(r - 1) + 1$$

The DFs in the formulas below are replaced with 10 and 20, respectively, to obtain the minimum and maximum numbers of animals required:

$$\text{Minimum } N = 10/(r - 1) + 1$$

$$\text{Maximum } N = 20/(r - 1) + 1.$$

Whenever the experiment involves sacrificing the animals at each repetition,  $N$  must be multiplied by  $r$ .

For example, in an experiment to study the effect of a drug on tumor sizes in a group of animals at four time points (pre-treatment, and post-treatment 1, 2, and 3), the sample sizes are:

$$\text{Minimum } N = 10/(4 - 1) + 1 = 4.3 = \text{rounded up to 5 animals}$$

$$\text{Maximum } N = 20/(4 - 1) + 1 = 7.7 = \text{rounded down to 7 animals}$$

Again, please note that the minimum and maximum numbers of animals are rounded up and down, respectively, to keep the DF for each sample size between the range of 10 and 20.

If the animals must be sacrificed at each measurement, the total sample sizes are:

$$\text{Minimum } N \times r = 5 \times 4 = 20 \text{ animals}$$

$$\text{Maximum } N \times r = 7 \times 4 = 28 \text{ animals}$$

*Design 3: Group comparison, repeated measures—one between and one within factor, repeated-measures ANOVA*

For repeated-measures ANOVA with one between-subject factor (the group), there are two error DFs: between-subject error DF and within-subject error DF (11).

The between-subject error DF is calculated as:

$$DF = N - k = kn - k = k(n - 1),$$

and the within-subject error DF in this ANOVA design is calculated as:

$$DF = (N - k)(r - 1) = (kn - k)(r - 1) = k(n - 1)(r - 1)$$

Thus, the error DF is the sum of these two error DFs:

$$\begin{aligned} DF &= \text{Between-subject error DF} + \\ &\text{Within-subject error DF} \\ &= k(n - 1) + k(n - 1)(r - 1) = \\ &k(n - 1)(1 + r - 1) = kr(n - 1), \end{aligned}$$

where  $N$  = total number of subjects,  $k$  = number of groups,  $n$  = number of subjects per group, and  $r$  = number of repeated measurements.

By rearranging the terms,  $n$  is obtained as:

$$n = DF/kr + 1$$

Similarly, the DFs in the following formulas are replaced with 10 and 20 for the minimum and maximum  $n$  and  $N$ , respectively. The minimum and maximum numbers of animals required are:

$$\text{Minimum } n = 10/kr + 1$$

$$\text{Maximum } n = 20/kr + 1$$

The minimum and maximum total numbers of animals required are:

$$\text{Minimum } N = \text{Minimum } n \times k$$

$$\text{Maximum } N = \text{Maximum } n \times k$$

Again, whenever the experiment involves sacrificing the animals at each repetition,  $n$  and  $N$  must be multiplied by  $r$ .

For example, consider a study that aims to compare three treatment groups (honey, honey with chemical, and control) with four repeated measurements (pre-treatment, and post-treatment 1, 2, and 3) of tumor sizes. Considering the error DF, the sample sizes per group are:

$$\text{Minimum } n = 10/(3 \times 4) + 1 = 1.8 = \text{rounded up to 2 animals/group}$$

$$\text{Maximum } n = 20/(3 \times 4) + 1 = 2.6 = \text{rounded down to 2 animals/group,}$$

resulting in equal sample sizes for the minimum and maximum  $N$ :

$$\text{Minimum (Maximum) } N = \text{Minimum (Maximum) } n \times 3 = 2 \times 3 = 6 \text{ animals}$$

If the animals must be sacrificed at each measurement, the total sample size is:

$$\text{Minimum (Maximum) } N \times r = 6 \times 4 = 24 \text{ animals}$$

## Closing Remarks

This article presented sample size formulas for three common ANOVA designs that are applicable to animal studies. The main formulas by the ANOVA designs are presented again in Table 1 as a quick reference. The focus of

this article is on the minimum and maximum numbers of animals required in an animal research. Given ethical consideration and budget limitations, a researcher may choose a suitable sample size for his or her planned animal study based on these simple formulas.

**Table 1.** Sample size formulas for three ANOVA designs

ANOVA design	Application	Minimum $n/\text{group}$	Maximum $n/\text{group}$
One-way ANOVA	Group comparison	$10/k + 1$	$20/k + 1$
One within factor, repeated-measures ANOVA	One group, repeated measurements	$10/(r - 1) + 1^{a,b}$	$20/(r - 1) + 1^{a,b}$
One-between, one within factor, repeated-measures ANOVA	Group comparison, repeated measurements	$10/kr + 1^b$	$20/kr + 1^b$

$k$  = number of groups,  $n$  = number of subjects per group,  $N$  = total number of subjects,  $r$  = number of repeated measurements. <sup>a</sup> $n = N$ , because only one group is involved, <sup>b</sup> $n$  must be multiplied by  $r$  whenever the experiment involves sacrificing the animals at each measurement.

## Authors' Contributions

Conception and design: WNA, WMZ  
 Analysis and interpretation of the data: WNA, WMZ  
 Drafting of the article: WNA, WMZ  
 Critical revision of the article for important intellectual content: WNA, WMZ  
 Final approval of the article: WNA, WMZ  
 Statistical expertise: WNA, WMZ

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